



**NATIONAL OPEN UNIVERSITY OF NIGERIA**  
**PLOT 91, CADASTRAL ZONE, NNAMDI AZIKIWE EXPRESSWAY, JABI - ABUJA**  
**FACULTY OF SCIENCES**  
**DEPARTMENT OF PHYSICS**  
**2025\_2 EXAMINATIONS**

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**COURSE CODE:** PHY 307  
**COURSE TITLE:** SOLID STATE PHYSICS I  
**CREDIT UNIT:** 2  
**TIME ALLOWED:** (2 HRS)  
**INSTRUCTION:** *Answer question 1 and any other two questions*

**QUESTION 1**

- (a). Define the term Crystal binding (2 marks)
- (b). What are Miller indices? (2 marks)
- (c). State the rules for determining Miller indices (4 marks)
- (d). Let the interaction energy between two atoms be given by:  $E(r) = -\frac{A}{r^2} + \frac{B}{r^8}$ . If the atoms form a stable molecule with an inter-nuclear distance of 0.4 nm and a dissociation energy of 3 eV, calculate A and B. (10 marks)
- (e). For an orbital of number N electrons in a sphere of radius  $k_F$ , and if there are two available spin states for a given set of  $k_x$ ,  $k_y$ , and  $k_z$ , show that the relationship between N and  $k_F$  and the density of states are  $k_F = \left(\frac{3\pi^2 N}{V}\right)^{1/3}$  and  $D(E) = \frac{3N}{2E}$ , respectively. (12 marks)

**QUESTION 2**

- (a). Write short note on the following terms: (i) Simple cubic lattice (ii) Body-Centered cubic Lattice (iii) Face- Centered Cubic Lattice (6 marks)
- (b). If the x-, y-, and z-, are intercepts are 2, 1, and 3, calculate the Miller indices (6 marks)
- (c). Show that  $\sqrt{3}\pi/8$  of the available volume is occupied by hard sphere in contact in a body centered cubic arrangement. (8 marks)

**QUESTION 3**

- (a). Define Lattice vibration (2 marks)
- (b). What is harmonic approximation? and state the condition the must be met before it can hold. (3 marks)
- (c). The energy of interaction of two atoms a distance r apart can be written as:

$$E(r) = \frac{a}{r} + \frac{b}{r^7}, \text{ where } a \text{ and } b \text{ are constants. Show that for the particles to be in equilibrium,}$$

$$r = r_0 = \left(\frac{7b}{a}\right)^{1/6} \quad (6\text{marks})$$

(d). The force of attraction between ions of Na and Cl is  $3.02 \times 10^{-9} \text{ N}$  when the two ions just touch each other. Given: ionic radius of  $\text{Na}^+$  ion is  $0.95 \text{ \AA}$ ,  $e = 1.6 \times 10^{-19} \text{ C}$ ,  $\epsilon_0 = 8.854 \times 10^{-12} \text{ C}^2 / \text{N} - \text{m}^2$ . Find the radius of  $\text{Cl}^-$  ion. (9 marks)

#### QUESTION 4

(a). Define Energy band (1 marks)

(b). Explain the following in terms of energy bands : (i) Insulators (ii) Semiconductors (6 marks)

(c). Solid Ar has an fcc structure with cubic lattice constant  $a = 5.26 \text{ \AA}$ , atomic mass  $M_{\text{AR}} = 6.67 \times 10^{-26} \text{ N/m}^2$  and a Debye temperature  $\theta_D = 92^0 \text{ K}$ . Estimate the phonon velocity using the Young modulus of  $C_{11} = 1.6 \times 10^9 \text{ N/m}^2$ . (6 marks)

(d). Einstein's model of solids gives the expression for the specific heat

$$C_v = 3N_0K \left(\frac{\theta_E}{T}\right)^2 \frac{e^{\theta_E/T}}{(e^{\theta_E/T} - 1)^2}$$

where  $\theta_E = hv/k$ . The factor  $\theta_E$  is called the characteristic temperature. Show that (a) at high temperatures Dulong Petit law is reproduced. (b) But at very low temperatures the  $T^3$  law is not given. (7 marks)

#### QUESTION 5

(a). Discuss Meissner effect in solids (4 marks)

(b). State Pauli principle (2 marks)

(c). At room temperature,  $\frac{k_B T}{e} = 26 \text{ mV}$ . A sample of cadmium sulfide displays a mobile carrier density of  $10^{16} \text{ cm}^{-3}$  and a mobility coefficient  $\mu = 10^2 \text{ cm}^2 / \text{volt sec}$

(i) Calculate the electrical conductivity of this sample.

(ii) If the charge carriers have an effective mass equal to 0.1 times the mass of a free electron, what is the average time between successive scatterings. (6 marks)

(d). If  $N_d$  and  $N_a$  are the donor and acceptor impurity density of an extrinsic semiconducting material, show that the density of hole  $h$  and density of electron are related as in (all symbols represent usual meanings )

$$n \approx (N_d - N_a) \text{ when } (N_d - N_a) \gg n_i \text{ and } p = (N_a - N_d) \text{ when } (N_a - N_d) \gg n_i \quad (8 \text{ marks})$$