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NATIONAL OPEN UNIVERSITY OF NIGERIA
University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi, Abuja
FACULTY OF SCIENCES
DEPARTMENT OF MATHEMATICS
2023_1 POP EXAMINATION

## Course Code: MTH 381

Course Title: MATHEMATICAL METHODS III
Credit Unit: 3
Time Allowed: 3 Hours
Total: 70 Marks
Instruction: Answer Question One (1) and Any Other 3 Questions

Q1 (a) Define each of the following:
i) a scalar function
ii) a differentiable vector function
(b) If $A=\left(3 x^{2}+6 y\right) i-14 y z j+20 x z^{2} k$, evaluate $\int_{C} A \cdot d r$ from $(0,0,0)$ to $(1,1,1)$.
(c) Is $f(z)=z^{3}$ analytic?
d) Show that $\oint_{c} \frac{d z}{z}=2 \pi i$
(e) State the Cauchy's integral formula.

Q2 (a) Define a function of two variables
(b) Find the Jacobian $\frac{\partial(u, v)}{\partial(x, y)}$ of $u=x^{2}+y^{2}, v=2 x y$
c) Define a stationary steady- state vector field.
(4 marks)
(5 marks)
(4 marks)
(3 marks)
(7marks)
(5 marks)

Q3 (a) Define whether $v(x)=\cos b x$ and $u(x)=\sin b x$ with $b \neq 0$ are linearly dependent or Independent
(b) Find the Jacobian $\frac{\partial(u, v)}{\partial(x, y)}$ of $u=x^{2}+y^{2}, v=2 x y$. (8marks)

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Q4 (a) Define a function of two variables. (3 marks)
(b) What is the relationship between vector field and vector functions? (4 marks)
c) Evaluate $\int_{-2}^{2} \int_{0}^{z} \int_{x-z}^{x+z}(x+y+z) d y d x d z$ ( $\mathbf{8}$ marks)

Q5. (a) Define whether $v(x)=\operatorname{cosb} x$ and $u(x)=\sin b x$ with $b \neq 0$ are linearly dependent or independent. ( 7 marks)
(b) Show that $f(z)=z^{3}$ satisfies the Cauchy- Riemann equations? ( $\mathbf{8}$ marks)

Q6(a) Define each of the following:
(i) derivative of a complex function ( $\mathbf{5}$ mark)
(ii) a differentiable complex function at a point ( $\mathbf{5}$ marks)
(b) if $z_{1}=3-4 i$ and $z_{1}=5+2 i$. Find $\frac{z_{1}}{z_{2}}$ ( 5 marks)

