NATIONAL OPEN UNIVERSITY OF NIGERIA University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi, Abuja FACULTY OF SCIENCES DEPARTMENT OF MATHEMATICS 2023_1 POP EXAMINATION...

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Course Code: MTH 381 Course Title: MATHEMATICAL METHODS III Credit Unit: 3 Time Allowed: 3 Hours Total: 70 Marks Instruction: Answer Question One (1) and Any Other 3 Questions

Q1 (a) Define each of the following:

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i)	a scalar function	(2 marks)
ii)	a differentiable vector function	(2 marks)

(b) If $A = (3x^2 + 6y)i - 14yzj + 20xz^2k$, evaluate $\int_C A \cdot dr$ from (0,0,0) to (1,1,1).

	(8 marks)
(c) Is $f(z) = z^3$ analytic?	(4 marks)
d) Show that $\oint_c \frac{dz}{z} = 2\pi i$	(5 marks)
(e) State the Cauchy's integral formula.	(4 marks)
Q2 (a) Define a function of two variables	(3 marks)
(b) Find the Jacobian $\frac{\partial(u,v)}{\partial(x,y)}$ of $u = x^2 + y^2$, $v = 2xy$	(7marks)
c) Define a stationary steady- state vector field.	(5 marks)

Q3 (a) Define whether v(x) = cosbx and u(x) = sinbx with $b \neq 0$ are linearly dependent or Independent (7 marks)

(b) Find the Jacobian $\frac{\partial(u,v)}{\partial(x,y)}$ of $u = x^2 + y^2$, v = 2xy. (8marks)

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Q4 (a) Define a function of two variables. (3 marks)

(b) What is the relationship between vector field and vector functions? (4 marks)

c) Evaluate $\int_{-2}^{2} \int_{0}^{z} \int_{x-z}^{x+z} (x+y+z) dy dx dz$ (8 marks)

- Q5. (a) Define whether v(x) = cosbx and u(x) = sinbx with $b \neq 0$ are linearly dependent or independent. (7 marks)
 - (b) Show that $f(z) = z^3$ satisfies the Cauchy-Riemann equations? (8 marks)

Q6(a) Define each of the following:

- (i) derivative of a complex function (**5 mark**)
- (ii) a differentiable complex function at a point (5 marks)

(b) if $z_1 = 3 - 4i$ and $z_1 = 5 + 2i$. Find $\frac{z_1}{z_2}$ (5 marks)