

direction of  $(v)$  given by  $(L=\{x+\alpha v: \alpha \in \mathbb{R}\})$  is a \_\_\_\_\_ convex set

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[MTH412] Let  $(p \leq 1)$  be a fixed real number. Each element in the space  $(l_p)$  is a sequence,  $(x = (x_1, x_2, \dots, x_k, \dots))$  of real numbers that converge then,  $(\sum_{k=1}^{\infty} |x_k|_p) < \infty$

[MTH412]  $(a \times k_2 \leq k \times k_1)$  vector space

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[MTH412] The real line  $\mathbb{R}$  becomes a normed linear space if  $(\| \cdot \|)$  is set to be \_\_\_\_\_ for every number  $(x \in \mathbb{R})$ .  $|x|$

[MTH412] Let  $(\| \cdot \|_1)$  and  $(\| \cdot \|_2)$  be two norms defined on a linear space  $(X)$  and  $(\| \cdot \|_1)$  and  $(\| \cdot \|_2)$  are called equivalent if there exist constants  $a, b > 0$  such that \_\_\_\_\_  $(a \times \| \cdot \|_1 \geq 0)$

[MTH412] All norms defined on a finite dimensional space are \_\_\_\_\_ normal