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## NATIONAL OPEN UNIVERSITY OF NIGERIA Plot 91, Cadastral Zone, Nnamdi Azikiwe Expressway, Jabi, Abuja.

## FACULTY OF SCIENCES April Examination 2019

Course Code: Course Title: Credit Unit: Time Allowed: Total: Instruction:	MTH301 Functional Analysis I 3 3 HOURS 70 Marks ATTEMPT NUMBER ONE (1) AND ANY OTHE	ER FOUR (4) QUESTIONS
(ii) Dis		(4 Marks) (7 Marks)
(c) Define separable set.		(4 Marks)
<ul> <li>(d) Prove that Q<sup>n</sup> is separable.</li> <li>2. (a) Define open ball (ε-neighbourhood)</li> <li>(b) Let x ∈ ℝ<sup>n</sup>, then show that the set B(x, ε) is open.</li> </ul>		(7Marks) (5Marks) (7Marks)
<ul> <li>3. (a) Define boundary point</li> <li>(b) (i) Define closure of subset S of a set X.</li> <li>(ii) Is the closure of S normally denoted by \$\overline{S}\$ closed or open? Justify</li> </ul>		(5Marks) (7Marks)
4. (a) When is a map $f: A \to B$ (metric spaces) said to be continuous? (5Marks)		
-	$A \rightarrow B$ between metric spaces is continuous if and only B = (7Morks)	if $f^{-1}(V)$ is open set in A whenever
<i>V</i> is open set in 5. (a) When is a sequer	B. (7Marks) nee of points $x_n$ in a metric space $(X, d)$ said to be com-	vergent to a point $x \in X$ .

(5Marks)

(b) Let (X, d) be a metric space. Prove that A of X is closed in (X, d) if and only if every convergent sequence of points in A converges to a point in A. (7Marks)

6. Let X be a metric space and let Y be a subspace of X then prove
(a) If X is compact and Y is closed in X, then Y is compact . (7Marks)
(b) If Y is compact, then it is closed in X. (5Marks)