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NATIONAL OPEN UNIVERSITY OF NIGERIA University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi-Abuja

FACULTY OF SCIENCES DEPARTMENT OF MATHEMATICS 2021_2 Examinations...

Course Code: MTH 305

Credit Unit: 3

Course Title: Complex Analysis II

| Time Allowed: 3 Hours Total: 70 Marks Instruction: Answer Question One (1) and Any Other 4 Questions | |
|--|-----------|
| Q1 (a) (i) Define a single-valued complex function $w(z)$. | (2 marks) |
| (ii) If $z \in C$ and $w(z)$. Suppose $f(z) = z^2$, find $u(x, y)$ and $v(x, y)$, | (4 marks) |
| (b) Define each of the following: | |
| (i) a continuous function f at a point z_0 . | (3 marks) |
| (ii) a branch point. | (2 marks) |
| (c) (i) Show that the function $u(x,y) = y^3 - 3x^2y$ is harmonic. | (4 marks) |
| (ii) Determine the poles and the residues at the poles of $f(z) = \frac{2z+1}{(z+1)(z-2z)}$ | (5 marks) |
| (d) State the Green's theorem in a plane. | (2 marks) |
| Q2 (a) Define a transformation. | (6 marks) |
| (b) Given that z is a complex number and $w = f(z)$. Find $\frac{1}{z}$. | (6 marks) |
| Q3 (a) Define the limit of a complex function $f(z)$. | (4 marks) |
| (b) Suppose $z \in C$. Show that $sin^2z + cos^2z = 1$. | (8 marks) |
| Q4 (a) Define each of the following: | |
| (i) removable singularities | (3 marks) |
| (ii) bounded complex function. | (2 marks) |

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(b) Prove that if
$$f(z) = \frac{\sin z}{z}$$
 then $z = 0$ is a removable singularity. (7 marks)

Q5 (a) State the residue theorem. (4 marks)

(b) Expand
$$f(z) = \frac{1}{z-3}$$
 in a Laurent series valid for $|z| > 3$. (8 marks)

Q6 (a) Define an analytic function
$$f(z)$$
. (3 marks)

(b) Establish that the real and imaginary part of the function $f(z) = z^2 + 5iz + 3 - i$ satisfy the Cauchy Riemann equation and deduce the analyticity of the function. (9 marks)