



**NATIONAL OPEN UNIVERSITY OF NIGERIA**

**UNIVERSITY VILLAGE, 91 CADASTRAL ZONE, NNAMDI AZIKWE EXPRESSWAY,  
JABI, ABUJA**

**FACULTY OF SCIENCE  
2021\_2 EXAMINATION<sup>48678</sup>**

**COURSE CODE: CIT756**

**COURSE TITLE: Operations Research**

**CREDIT: 2 Units**

**TIME ALLOWED: 2 Hours**

**INSTRUCTION: Answer Question ONE (1) and any other THREE (3) Questions**

1(a) Analyse the concept of problem definition in operation research [5 marks]

(b) Give the Differences between Critical Path Analysis (CPA) and Programme Evaluation and Review Technique (PERT) [4 marks]

(c) Assume a single channel service system of a library in a school. From past experiences it is known that on an average, every hour 8 students come for issue of the books at an average rate of 10 per hour. Determine the following:

(i). Probability of the assistant librarian being idle 2 marks

(ii). Probability that there are at least 3 students in the system 2 marks

(iii). Expected time that a student is in queue 2 marks

(d) State the steps involved in calculation of replacement policy when money value changes [5 marks]

(e) Analyse the behavior of customers while waiting in a queue [ 5 marks]

2(a) Analyse the concept of solution development in operation research [ [5 marks]

(b) A special diet for a patient in the hospital must have at least 8000 units of vitamins, 100 units of minerals and 2800 units of calories. Two types of foods X and Y are available in the market at the cost of #8 and #6 respectively. One unit of X contains 40 units of vitamins two units of minerals and 80 units of calories. One unit of food B contains 200 units of vitamins, four units of minerals and 80 units of calories. Form a mathematical model and state the constraints to find the combination of foods X and Y that can be used so that the minimum requirement of vitamins,

minerals and calories is maintained and the cost incurred by the hospital is minimised? [ 10 marks]

3 (a) Arrival rate of customers at a photocopying centre is according to Poisson distribution, with an average time of 12 minutes between two consecutive customers' arrival. The length of photocopying for each customer is assumed to be exponentially distributed with a mean of 4 minutes

(i). Determine the probability that a customer arriving at the centre will have to wait [2 marks]

(ii). Find the average queue length that is formed from time to time [2 marks]

(iii). The photocopying company will install second centre when convinced that an arrival would expect to have to wait at least 5 minutes for the photocopying. Find the increase in flows of arrivals which will justify a second centre. [3 marks]

(iv). What is the probability that a customer will have to wait for more than 15 minutes before the photocopying ? [2 marks]

(v). Find the fraction of a day that the photocopier will be in use. [1 mark]

(b) Analyse the reasons for replacing equipment

4(a) Demonstrate a flow that shows the steps involved in operation research [5 marks]

(b) A metal alloy used in the manufacture of rifles uses two ingredients A and B. A total of 120 units of alloy are used for production. Not more than 60 units of A can be used and at least 40 units of ingredient B must be used in the alloy. Ingredient A costs Rs. 4 per unit and ingredient B costs Rs. 6 per unit. The company manufacturing rifles is keen to minimise its costs. Formulate a mathematical model for the problem and state the constraints to the solution.

5 (a) Analyse the weakness of operation research [5 marks]

(b) Assuming a company found out that it is not importing its raw materials in the most economic way. A financial analysis shows that:

It cost #900.00 to make an order. Each item costs #50.50. The annual holding costs are 10 per cent of the price paid. The current annual consumption is 500,000.00

Determine the following:

i. The optimal order size.

ii. The number of days this supply would last.

iii. The number of orders per year? (Assume year = 250 working days)