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## NATIONAL OPEN UNIVERSITY OF NIGERIA University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi-Abuja

## FACULTY OF SCIENCES DEPARTMENT OF MATHEMATICS

Course Code: MTH422 Course Title: Partial Differential Equations Credit Unit: 3 Time Allowed: 3 Hours Total: 70 Marks Instruction: Answer Question One and Any Other Four Questions

Q1 (a) Define each of the following:

- i) a nth order partial differential equation (2 marks)
- ii) a linear partial differential equation (2 marks)
- iii) a slip (3 marks)

(b) Find the general solution of  $xz_x + yz_y = z$ . (8 marks)

(c) Given that xp + yq = pq. Find the initial element, if  $x = x_0, y = 0$  and  $z = \frac{x_0}{2}, z(x, 0) = \frac{x}{2}$ . (7 marks)

Q2 (a) State the conservation law

(b) Suppose u is the density of the substance and F is the flux, show that  $ut + a(u)u_x = 0$ .

(9 marks)

(3 marks)

Q3 (a) State the types of solutions a partial differential equation can have (3 marks)

(b) Consider z = px + qy + f(p, q), find the complete solution (9 marks)

Q4 (a) How can a second order semi-linear partial differential equation be classified? (3 marks)

(b) Given that 
$$z \frac{\partial^2 u}{\partial x \partial y} + 2x \frac{\partial^2 u}{\partial y \partial z} = 0$$
 is hyperbolic-parabolic in  $R^3$  and  

$$A_{ij} = \begin{pmatrix} 0 & z & 0 \\ z & 0 & x \\ 0 & x & 0 \end{pmatrix}.$$
 Find  $\lambda$ . (9 marks)

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Q5 (a) What is a well posed partial differential equation? (3 marks)

(b) Show that characteristics are invariant under regular transformation. (9 marks)

Q6 (a) Define an element of a stripe (2 marks)

(b) Copy and complete the following:

- i)  $x \frac{\partial z}{\partial y} + y \frac{\partial z}{\partial y} = cosxy$  is \_\_\_\_\_\_ order and \_\_\_\_\_ homogeneous PDE (2 marks)
- ii)  $\frac{\partial^2 u}{\partial x \partial y} + \left(\frac{\partial u}{\partial x}\right)^2 = \frac{\partial y}{\partial z} + z^3$  is \_\_\_\_\_\_ order and \_\_\_\_\_ linear PDE. (2 marks)
- iii)  $\frac{\partial^2 u}{\partial t} c^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) = 0$  is \_\_\_\_\_\_ order and \_\_\_\_\_\_ homogeneous PDE (2 marks)
- iv)  $\left(\frac{\partial^2 u}{\partial x^2}\right)^3 + \left(\frac{\partial^2 u}{\partial y^2}\right) + \frac{\partial^2 u}{\partial x \partial y} + \frac{\partial u}{\partial y} = 0$  is \_\_\_\_\_\_ order and \_\_\_\_\_ linear PDE (2 marks)

(c) Solve 
$$4(1 + z^3) = 9z^4pq$$
 (2 marks)