

NATIONAL OPEN UNIVERSITY OF NIGERIA Plot 91, Cadastral Zone, Nnamdi Azikwe Expressway. Jabi, Abuja. FACULTY OF SCIENCES DEPARTMENT OF MATHEMATICS 2020_2 EXAMINATION

Course Code: MTH 303 Course Title: MTH 303 Vector and Tensor Analysis Credit Unit: 3 Time Allowed: 3 Hours Instruction: Answer Question Number One and Any other Four Questions.

1. a) Find a unit vector parallel to the resultant of vectors $r_1 = 2i + 4j - 5k$ and $r_2 = i + 2j + 3k$ [4 Marks]

- b) Calculate the *curl* of the vector $\vec{f} = xyzi + 3x^2yj + (xz^2 y^2z)k$ [4 Marks]
- c) If A = i 2j 3k, B = 2i + j k and C = i + 3j 2k, find $A \bullet (B \times C)$. [5 Marks]
- d) If $f = f(x^1, x^2, x^3, ..., x^n)$, then show that $df = \frac{\partial f}{\partial x^i} dx^i$. [4 Marks]

e) Using Stoke's theorem or otherwise, evaluate $\int_C [(2x - y)dx - yz^2 dy - y^2 z dz]$ where *C* is the circle $x^2 + y^2 = 1$, corresponding to the surface of sphere of unit radius. [5 Marks]

2a) Determine λ and μ by using vectors, such that the points A, B and C are given as (-1, 3, 2), (-4, 2, -2) and $(5, \lambda, \mu)$ respectively lie on a straight line. [6 Marks] b) Evaluate $\iint_{\Re} \sqrt{x^2 + y^2} dx dy$, where \Re is the region bounded by $x^2 + y^2 = 4$ and $x^2 + y^2 = 9$ [6 Marks] 3a) If $A = (3x^2 + 6y)i - 14yzj + 20xz^2k$, evaluate $\int_C A \cdot dr$ from (0,0,0) to (1,1,1) along x = t, $y = t^2$ and $z = t^3$. [8 Marks] b) If the coordinates of P be (3, 4, 12), then find \overrightarrow{OP} , its magnitude and direction cosines. [4 Marks]

4a) Apply the divergence theorem to compute $\iint_{S} u \cdot n \, ds$ where *S* is the surface of the cylinder $x^2 + y^2 = a^2$ bounded by the planes z = 0, z = b and where u = xi - yj + zk. [6 Marks]

b) Let
$$F = \frac{-yi + xj}{x^2 + y^2}$$
. Calculate $\nabla \times F$ [6 Marks]

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| at $x = 0$, $y = 0$ and $z = 0$. | [8 Marks] |
|--|-----------|
| b) Write the covariant derivative with respect to x^q of this tensor A^{jk} | [4Marks] |
| 6. a) Evaluate $\int_{(0,1)}^{(1,2)} (x^2 - y) dx + (y^2 + x)$ along | |
| (i) a straight line from $(0, 1)$ to $(1, 2)$ | [3 Marks] |
| (ii) a straight lines from $(0, 1)$ to $(1, 1)$ and then from $(1, 1)$ to $(1, 2)$ and | [3 Marks] |
| (iii) the parabola $x = t$ and $y = t^2 + 1$. | [3 Marks] |

b) Express in matrix notation the transformation equations for a covariant vector $\overline{A}_q = \frac{\partial x^q}{\partial \overline{x}^p} A_q$ of rank two, assuming *N* = 3. [3 Marks]