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## NATIONAL OPEN UNIVERSITY OF NIGERIA University Village, Plot 91, Cadastral Zone, Nnamdi Azikwe Express Way, Jabi-Abuja

## FACULTY OF SCIENCES 2021 1 Examinations

Course Code: MTH315

Course Title: Analytical Dynamics

Credit Unit: 3

Time Allowed: 3 Hours Total: 70 Marks

horizontally?

**Instruction:** Answer Question One (1) and Any Other 4 Questions

- 1. (a) Determine the number of degrees of freedom in each of the following cases:
  - (i) 12 particles moving freely in a plane (ii) 23 particles moving freely in space.

(4 marks)

(8 marks)

- (b) A system of particles consists of a 2-gram mass located at (1, 0, -3), a 7-gram mass at (-1,1,3) and 2-gram mass at (1, -1, 1). Find the center of mass. (6 marks)
- (c) A uniform beam is 100m long and has a mass 100kg and masses of 60kg and 80 kg are suspended from its ends; at what point must the beam be supported so that it may rest

d) A quadrilateral ABCD has masses 1,5, 2 and 3 units located at its vertices, A(3,-2,2), B(2,-2,3), C(1,-2,4) and D(4,1,3). Find the coordinates of the center of mass (4 marks)

2. Three particles of masses 3,2,4 respectively have position vectors

$$r_1 = (t+2)i - 2t^2j + k,$$
  
 $r_2 = -2ti + 3t^2j + k,$   
 $r_3 = -\frac{1}{2}t^2i - ti + 2tk$  where  $t$  is

 $r_3 = \frac{1}{2}t^2i - tj + 2tk$ , where t is time.

- Find (a) the velocity of the center of mass at time t = 0 (b) the acceleration at t=1.(12 marks)
- 3. A particle of mass 10 units moves along a space curve whose position vector is given as a function of time *t* by

$$r = (2t^3 - 3t + 2)i + (6t^2 - t)j + t^3k$$

At time t = 1, find the (a) momentum (b) force field.

(12 marks)

- 4. A particle of mass 2 moves in a force field depending on time t given by  $F = 6t^2i 2tj + 4tk$ . Assuming that at t = 0 the particle is located at  $r_0 = 2i 3j + k$  and has velocity  $v_0 = i + 3j k$ , find (a) the velocity (b) the position at any time t. (12 marks)
- 5. A particle moves along the x axis in a force field having potential

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$$V = ax^2 - bx^3 + \frac{2}{3},$$

where a and b are positive constants. Determine the point(s) of equilibrium.

(12 marks)

6. (a) State without proof the Liouville's theorem in Hamiltonian theory. (4 marks)

(b) Minimise the integral

$$I = \int_0^{\frac{\pi}{2}} \left[ 3 \left( \frac{dy}{dt} \right)^2 - 3y^2 + 6ty \right] dt, y(0) = \frac{\pi}{2} \text{ and } y \left( \frac{\pi}{2} \right) = 0$$
 (8 marks)